

Learning Bayesian networks

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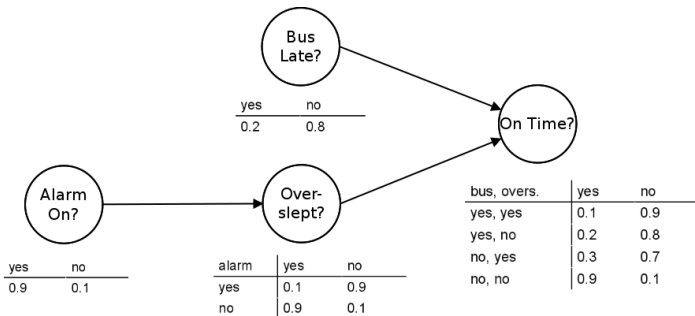
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Bayesian networks

- ▶ Representations of joint probability distributions
- ▶ Consist of:
 - ▶ The structure is a directed acyclic graph (DAG) that represents conditional independencies between variables
 - ▶ The local conditional probability distributions that are specified by parameters



Why are Bayesian networks useful?

- ▶ Compact
 - ▶ Number of parameters grows with the maximum number of parents
- ▶ Flexible
 - ▶ It is possible to compute any conditional probability
 - ▶ This is called *inference*
- ▶ Interpretable
 - ▶ Human expert can evaluate semantics and properties of the network



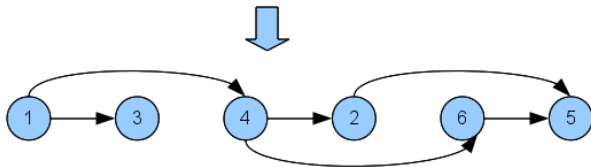
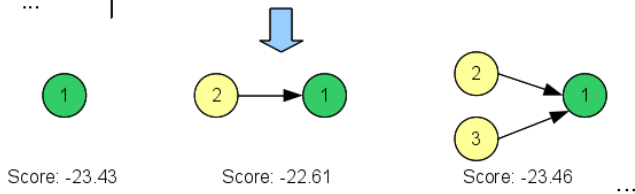
Learning Bayesian networks

- ▶ Input: samples from a multivariate probability distribution
- ▶ Learning the parameters of a Bayesian network
 - ▶ Given the structure, learning parameters is straightforward
 - ▶ Just use your favorite statistical principle (maximum likelihood, Bayesian, . . .)
- ▶ Learning the structure of a Bayesian network
 - ▶ The structure determines the parameters that are needed.
 - ▶ Thus, one can first learn the structure and then the parameters.
 - ▶ NP-hard in general



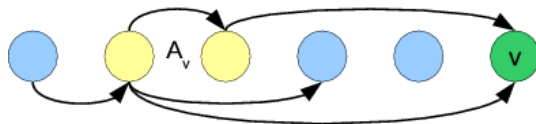
Score-based Structure Discovery

	Var. 1	Var. 2	Var. 3	Var. 4	...
Person A	1	1	2	1	
Person B	2	2	1	1	
Person C	1	2	2	2	
Person D	2	1	2	1	
...					



Research questions

- ▶ Exact learning of the structure
 - ▶ NP-hard, but doable for moderate-sized networks
- ▶ Learning Bayesian networks with bounded graph parameters
 - ▶ Motivation: Guarantee fast inference
- ▶ Heuristics with quality guarantees
 - ▶ Motivation: Exact algorithms are unlikely to scale-up into large networks



Thank you!

