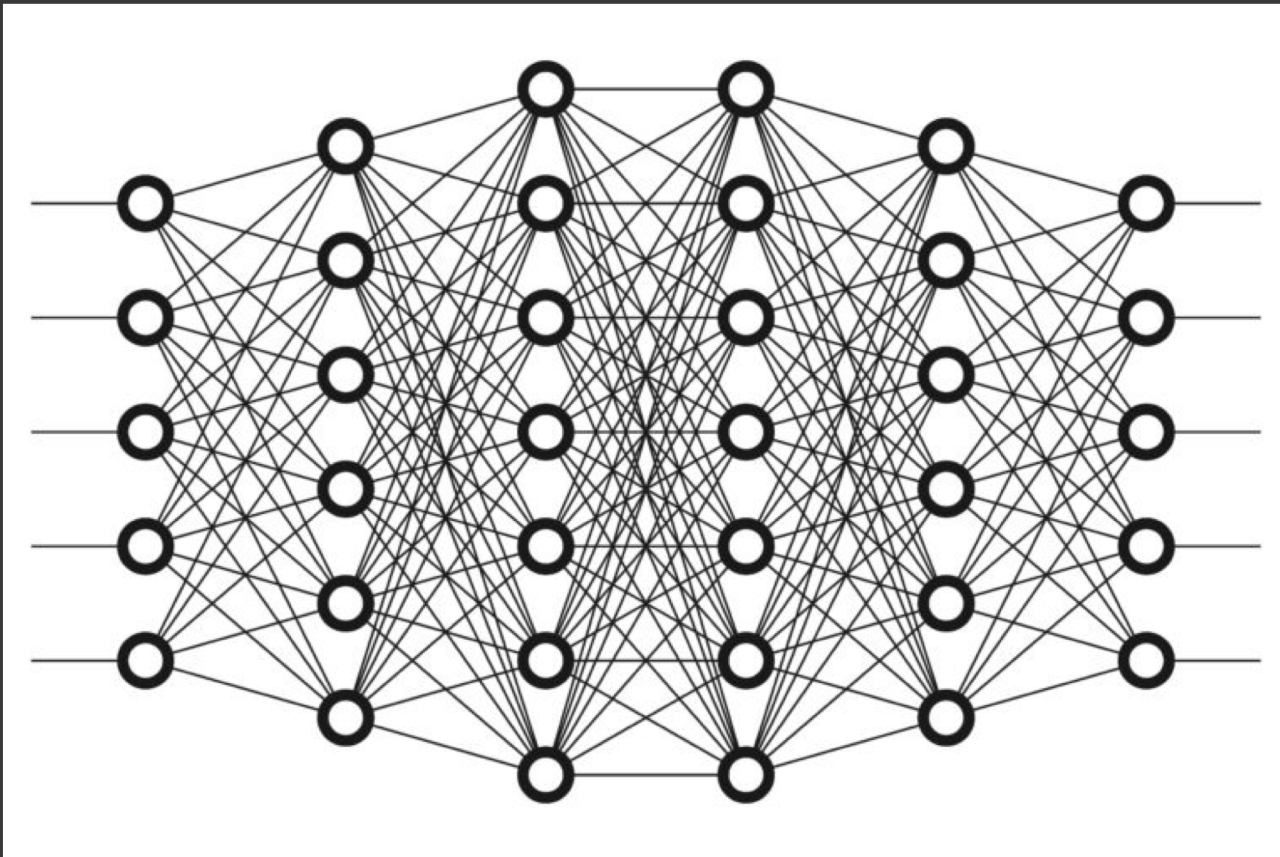




Introduction to the Tsetlin Machine
Ole-Christoffer Granmo
April 1, 2019

The complexity of neural networks



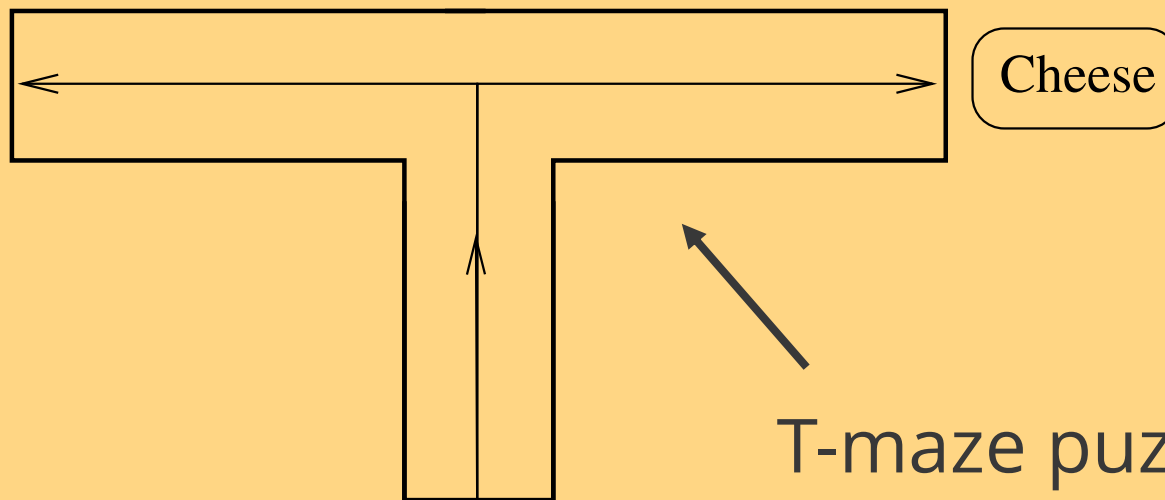
011011001110000111

Michael Lvovitch Tsetlin



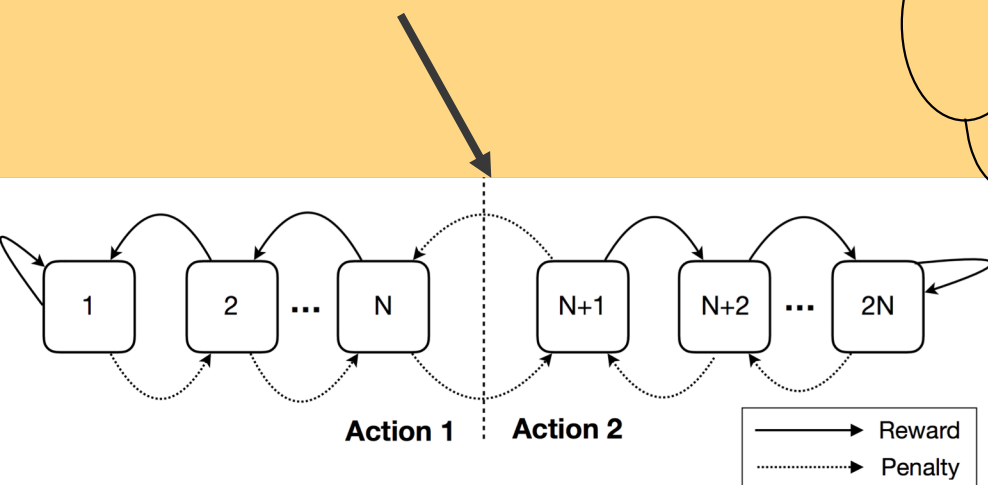
Michael Lvovitch Tsetlin (the surname is also written Cetlin, Tzetlin, Zeitlin, Zetlin; cyrillic: Михаил Львович Цетлин) (22 September 1924 – 30 May 1966) was a Russian mathematician and physicist who worked on cybernetics.

The Tsetlin automaton: A mathematical rat brain

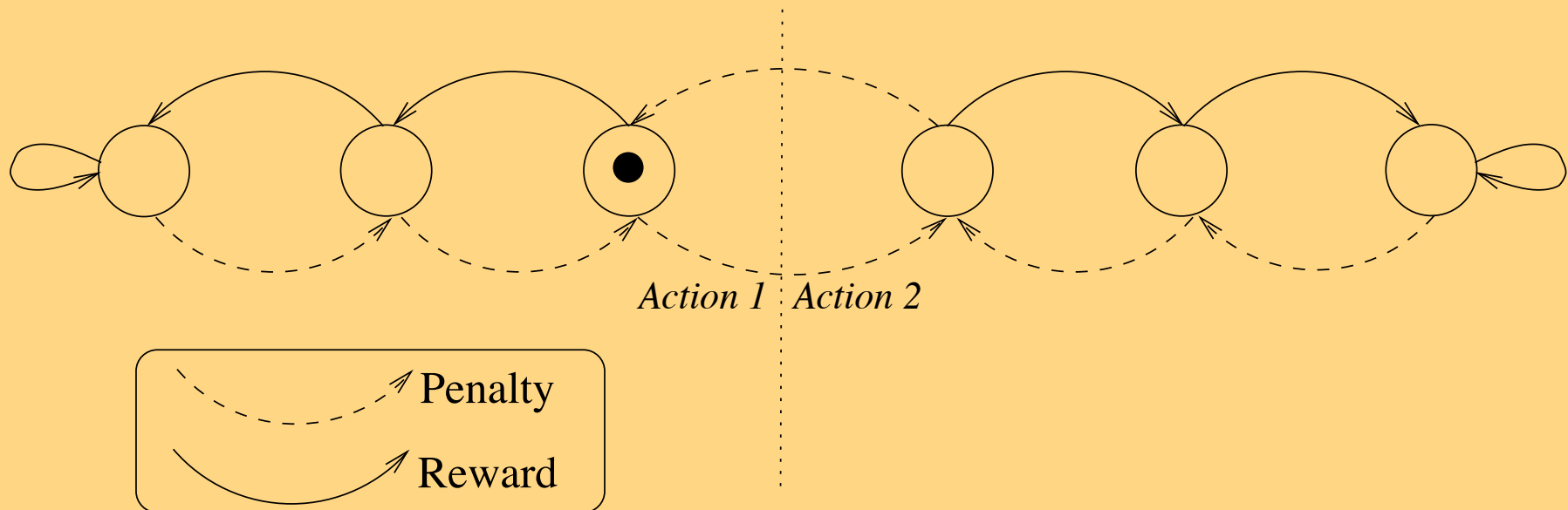


T-maze puzzle

Mathematical rat brain



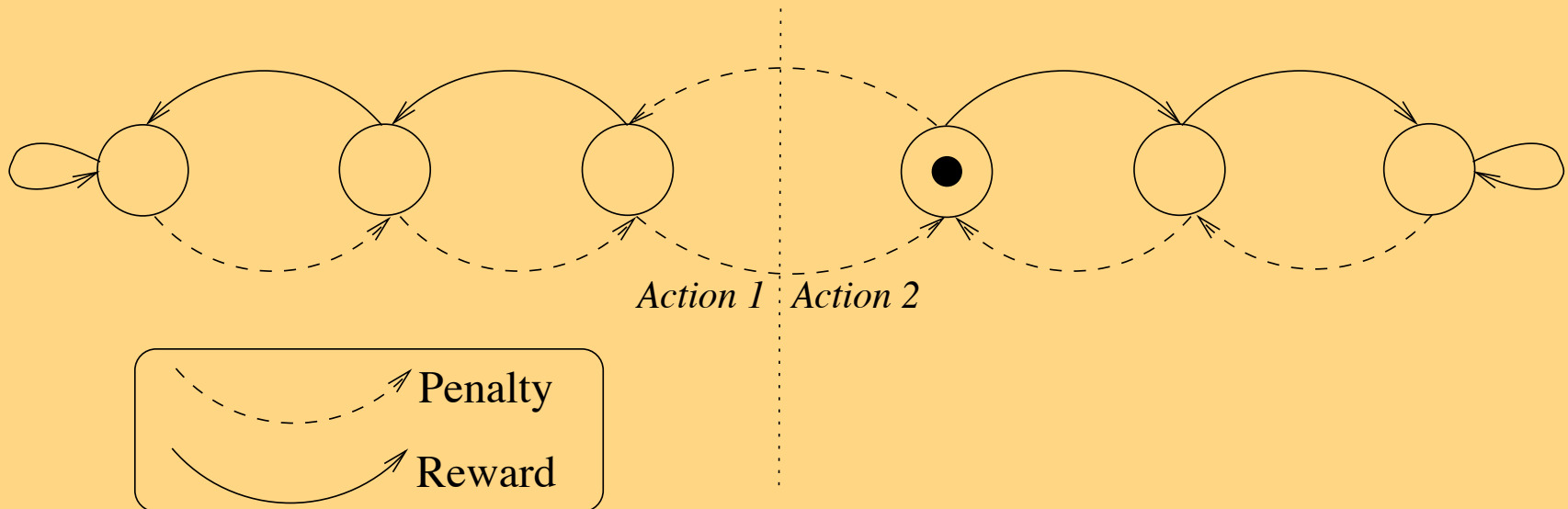
The Tsetlin automaton



Selected Action: Action 1

Response from Environment: Penalty

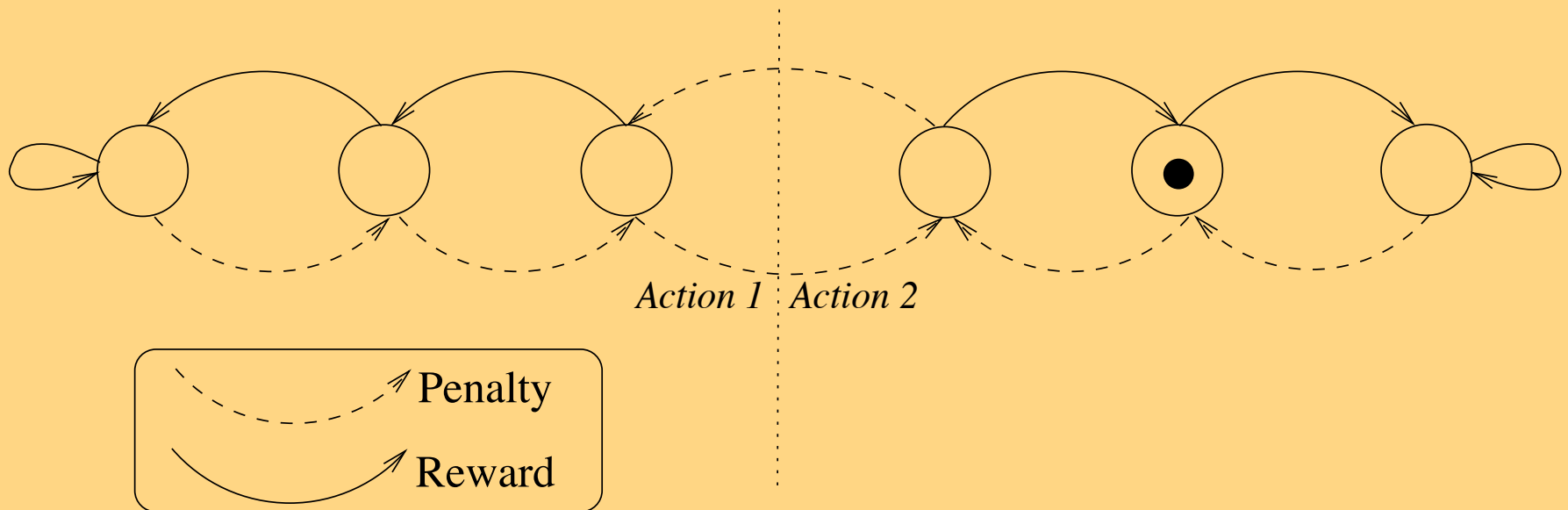
The Tsetlin automaton



Selected Action: Action 2

Response from Environment: Reward

The Tsetlin automaton



Selected Action: Action 2

Response from Environment: Reward

Propositional logic

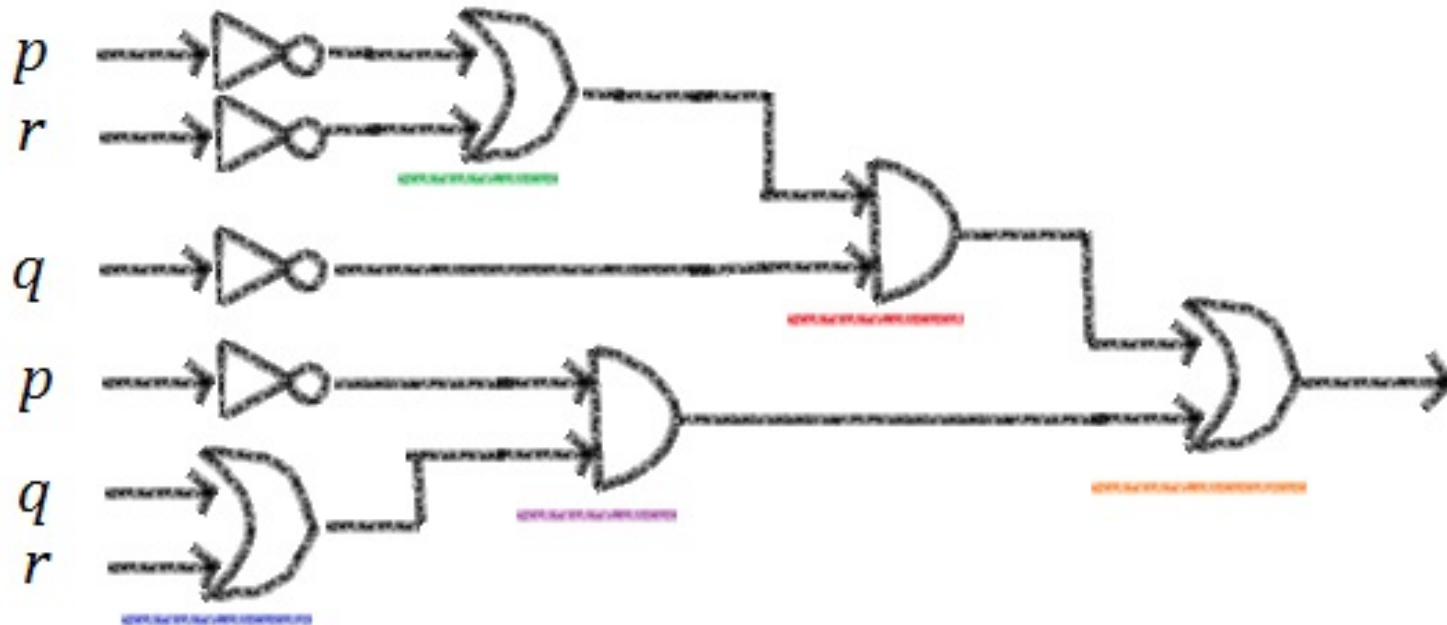


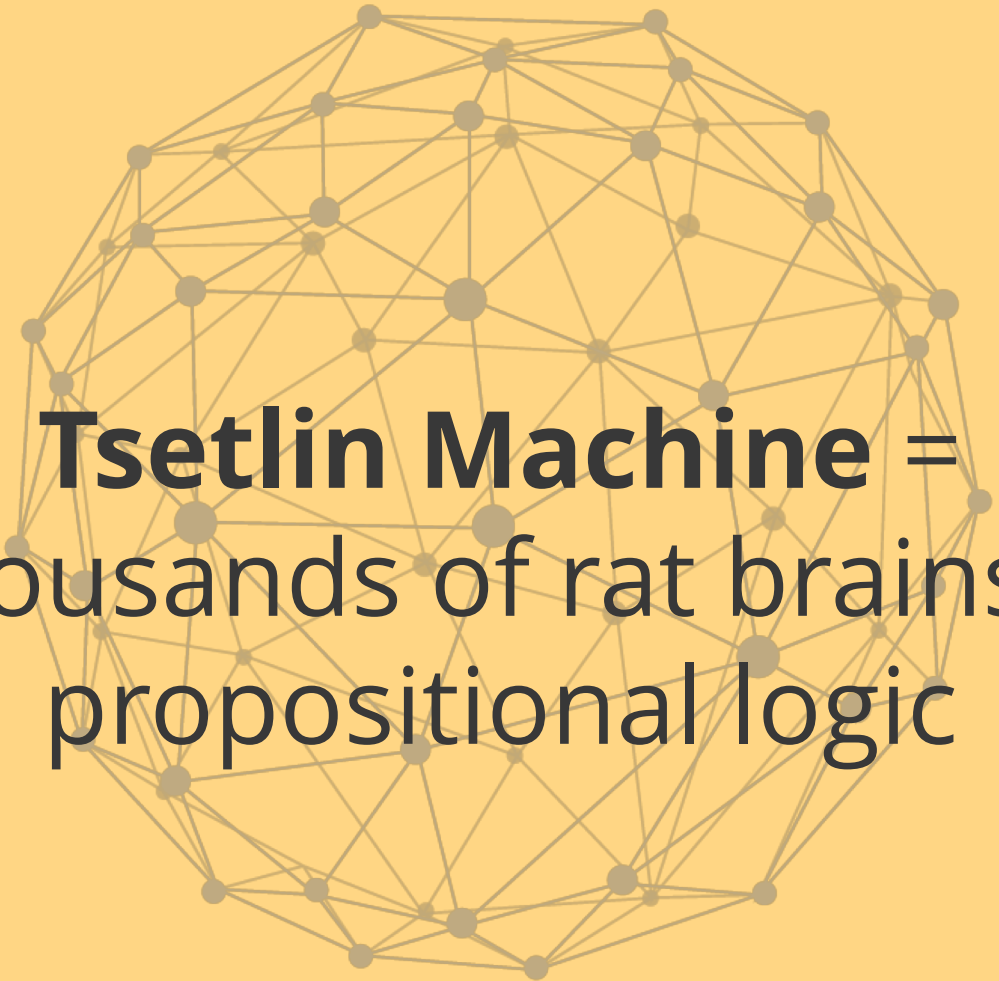
Propositional logic is the branch of logic that studies ways of joining and/or modifying entire propositions, statements or sentences to form more complicated propositions, statements or sentences, as well as the logical relationships and properties that are derived from these methods of combining or altering statements.

The Internet Encyclopedia of Philosophy

Propositional logic

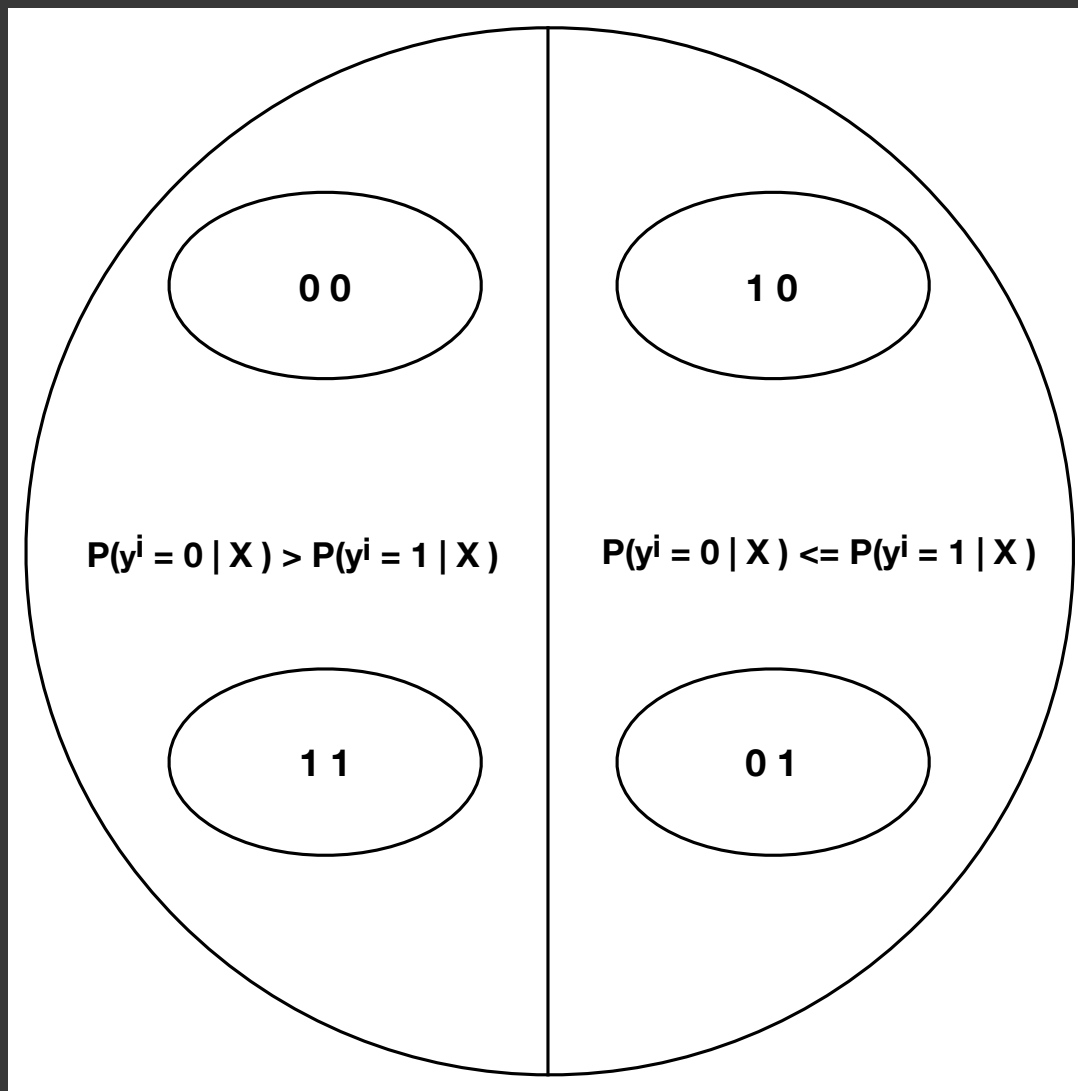
$$((\neg p \vee \neg r) \wedge \neg q) \vee (\neg p \wedge (q \vee r))$$





Tsetlin Machine =
thousands of rat brains +
propositional logic

The pattern recognition problem

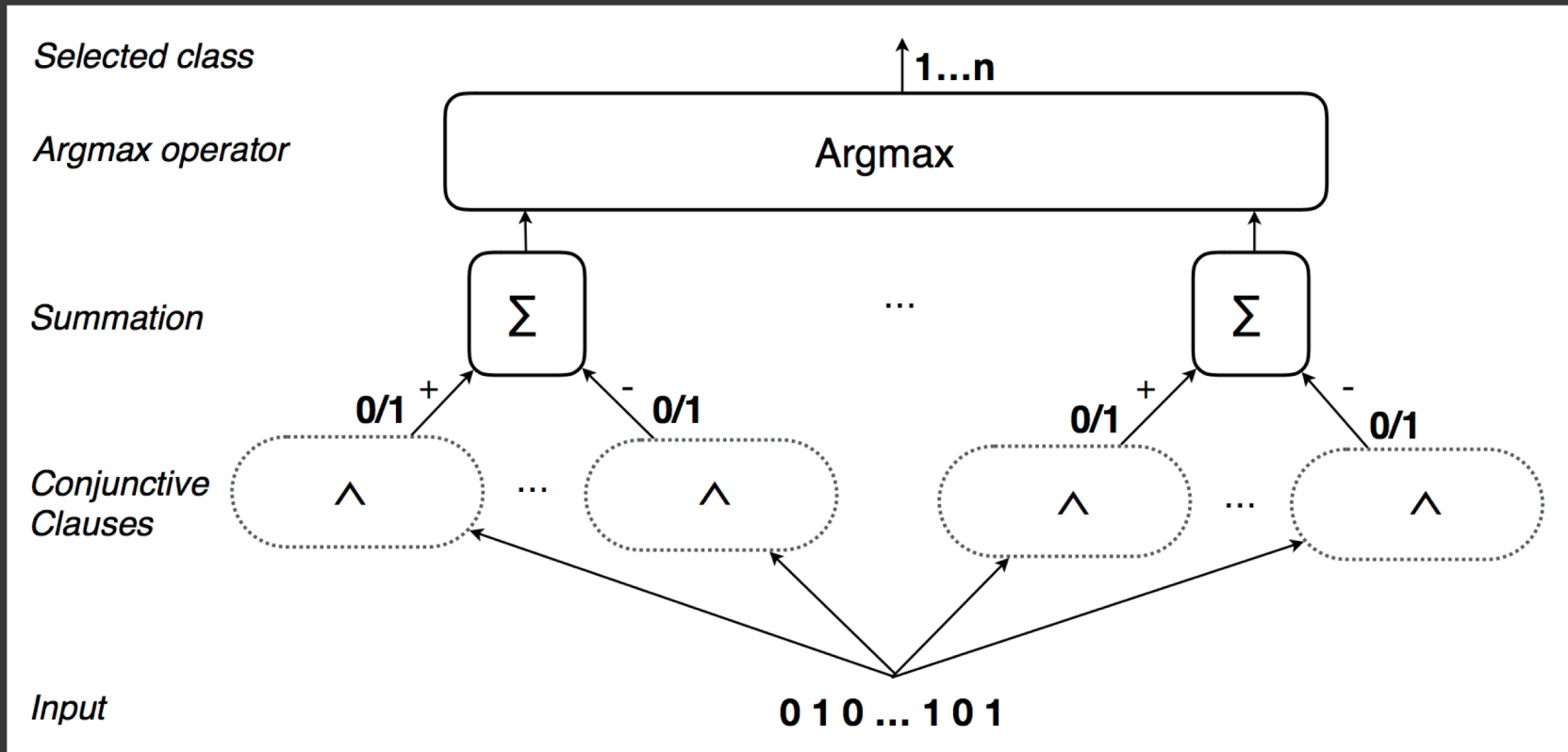


$$X = [x_1, x_2] \quad f(X) = (x_1 \wedge \neg x_2) \vee (\neg x_1 \wedge x_2)$$

The pattern recognition problem

Input	Target
010110110110	1
111010110011	0
001101111010	0
1010101111011	0
1110111101100	1
100000010110	1
111011100010	0
1010101111011	1
000011011100	0
100010110010	1

The Tsetlin Machine



<https://github.com/cair/TsetlinMachine>



Tsetlin Machine learning procedure

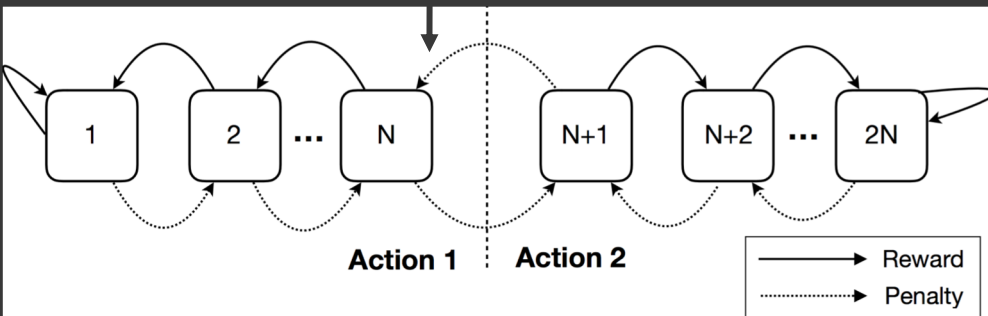
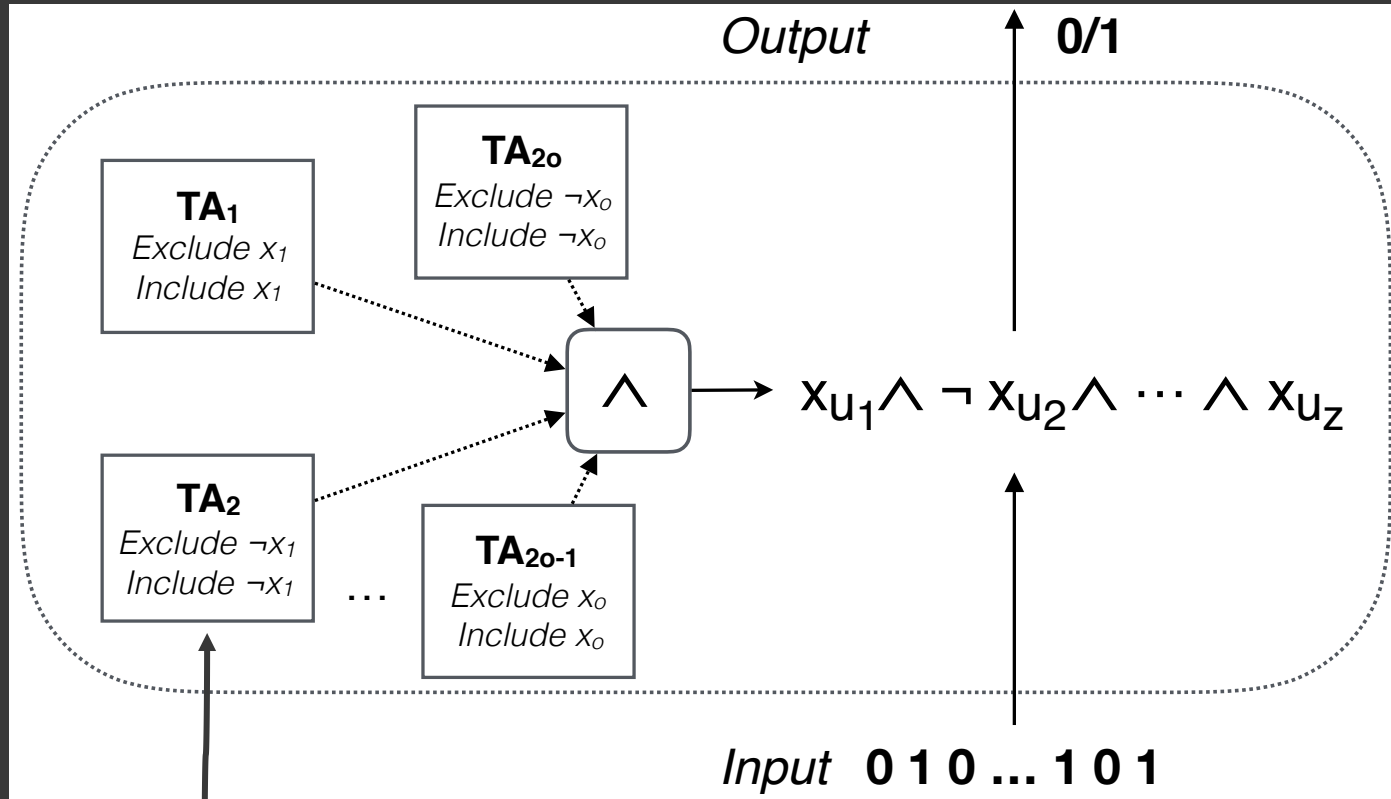
It's astounding that those things work at all...
it's like "pour Scrabble letters into box... shake
vigorously... open and read the answer!"

claytonkb, Reddit, February, 2019

The Tsetlin Machine game

1. The arrival of a labelled object (\hat{X}, \hat{y}) signals the start of a new game round.
2. Each Tsetlin Automaton decides whether to *include* or *exclude* its designated literal, leading to a new configuration of clauses $\underline{\mathbf{C}}$
3. Each clause, $C_j \in \underline{\mathbf{C}}$, is then evaluated with \hat{X} as input.
4. The final output, y , of the Tsetlin Machine is decided and compared with the target output \hat{y} .
5. Each Tsetlin Automaton is independently and randomly given either Reward, Inaction, Penalty feedback, based on a novel game matrix

The Tsetlin Machine: Clause formation as a **game**



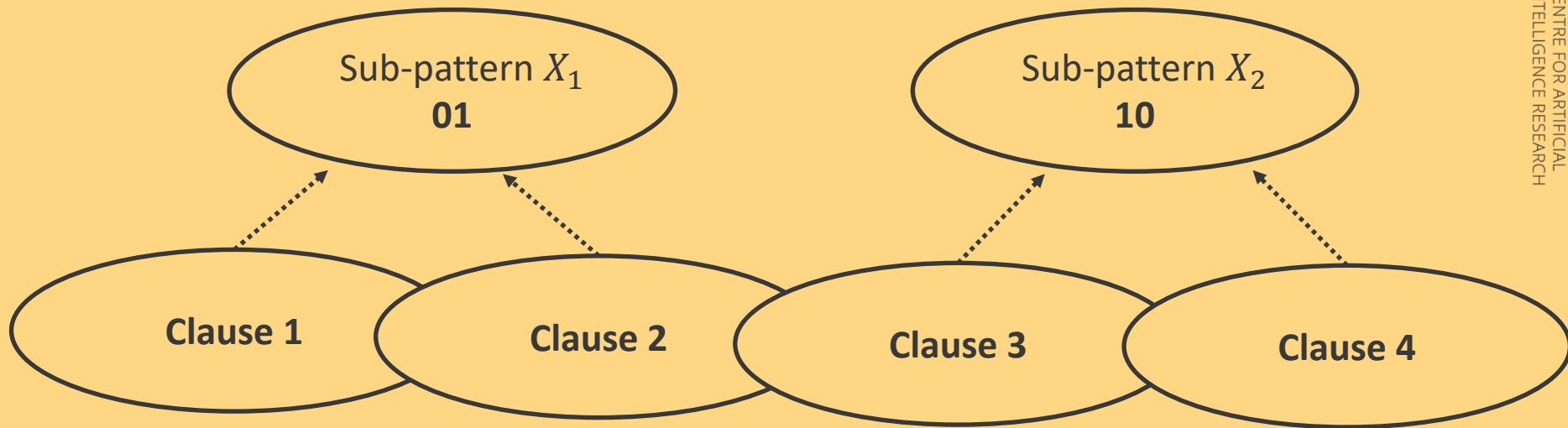
Type I feedback (true positive & false negative)

Document→	Target Clause evaluates to Target Literal evaluates to	1		0	
		1	0	1	0
Include literal	<i>P</i> (Reward)	$\frac{s-1}{s}$	NA	0	0
	<i>P</i> (Inaction)	$\frac{1}{s}$	NA	$\frac{s-1}{s}$	$\frac{s-1}{s}$
	<i>P</i> (Penalty)	0	NA	$\frac{1}{s}$	$\frac{1}{s}$
Exclude literal	<i>P</i> (Reward)	0	$\frac{1}{s}$	$\frac{1}{s}$	$\frac{1}{s}$
	<i>P</i> (Inaction)	$\frac{1}{s}$	$\frac{s-1}{s}$	$\frac{s-1}{s}$	$\frac{s-1}{s}$
	<i>P</i> (Penalty)	$\frac{s-1}{s}$	0	0	0

Type II feedback (false positive & true negative)

Document→	Target Clause evaluates to Target Literal evaluates to	1		0	
		1	0	1	0
Include literal	<i>P</i> (Reward)	0	NA	0	0
	<i>P</i> (Inaction)	1.0	NA	1.0	1.0
	<i>P</i> (Penalty)	0	NA	0	0
Exclude literal	<i>P</i> (Reward)	0	0	0	0
	<i>P</i> (Inaction)	1.0	0	1.0	1.0
	<i>P</i> (Penalty)	0	1.0	0	0

Allocation of sparse pattern representation resources



To effectively utilize sparse pattern representation capacity (a constrained number of clauses), we use a threshold value T as target for the summation $f_{\Sigma}(X)$. That is, the probability of activating *Type I Feedback* is:

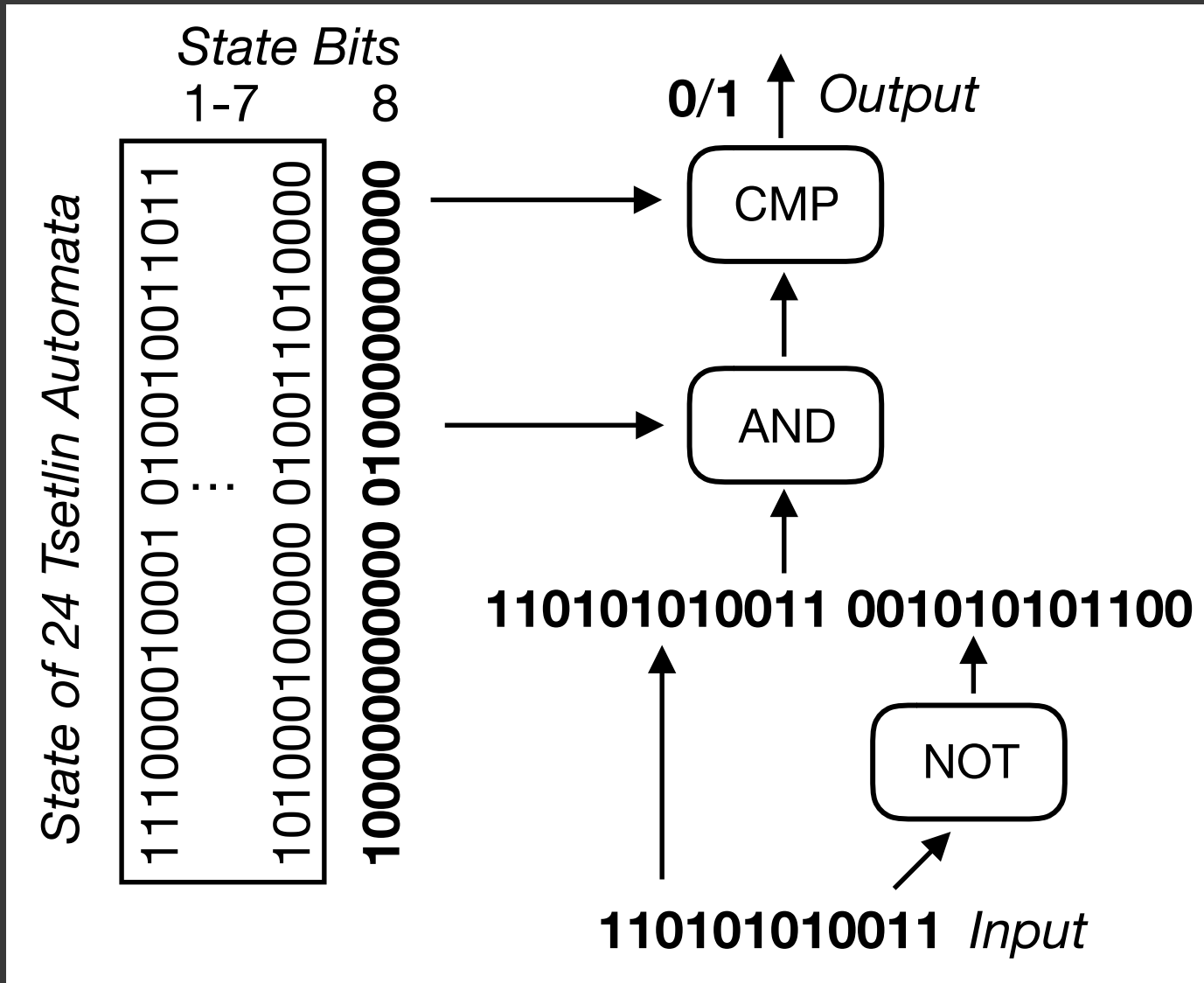
$$(T - \max(-T, \min(T, f_{\Sigma}(X)))/2T$$

while *Type II Feedback* is activated with probability:

$$(T + \max(-T, \min(T, f_{\Sigma}(X)))/2T$$

If the votes accumulate to a total of +/- T or more, neither rewards or penalties are handed out to the involved Tsetlin Automata.

Bit representation of clause



Bit representation of clause

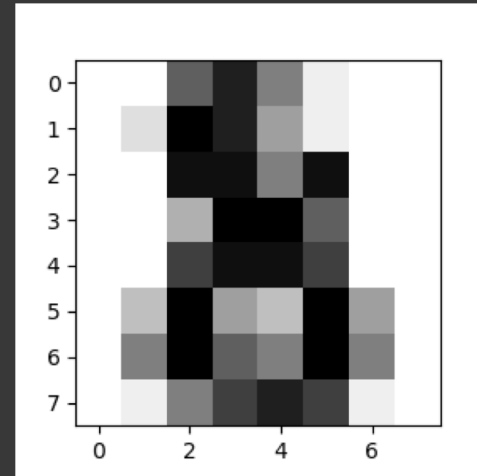
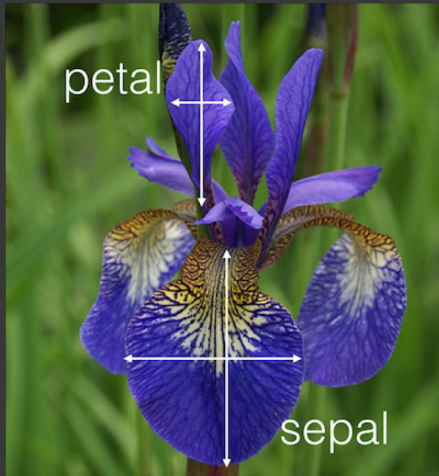
```
((*tm).ta_state[j][k][STATE_BITS-1] & Xi[k]) == (*tm).ta_state[j][k][STATE_BITS-1];
```

<https://github.com/cair/fast-tsetlin-machine-with-mnist-demo>



Applications and empirical results

Does it work?

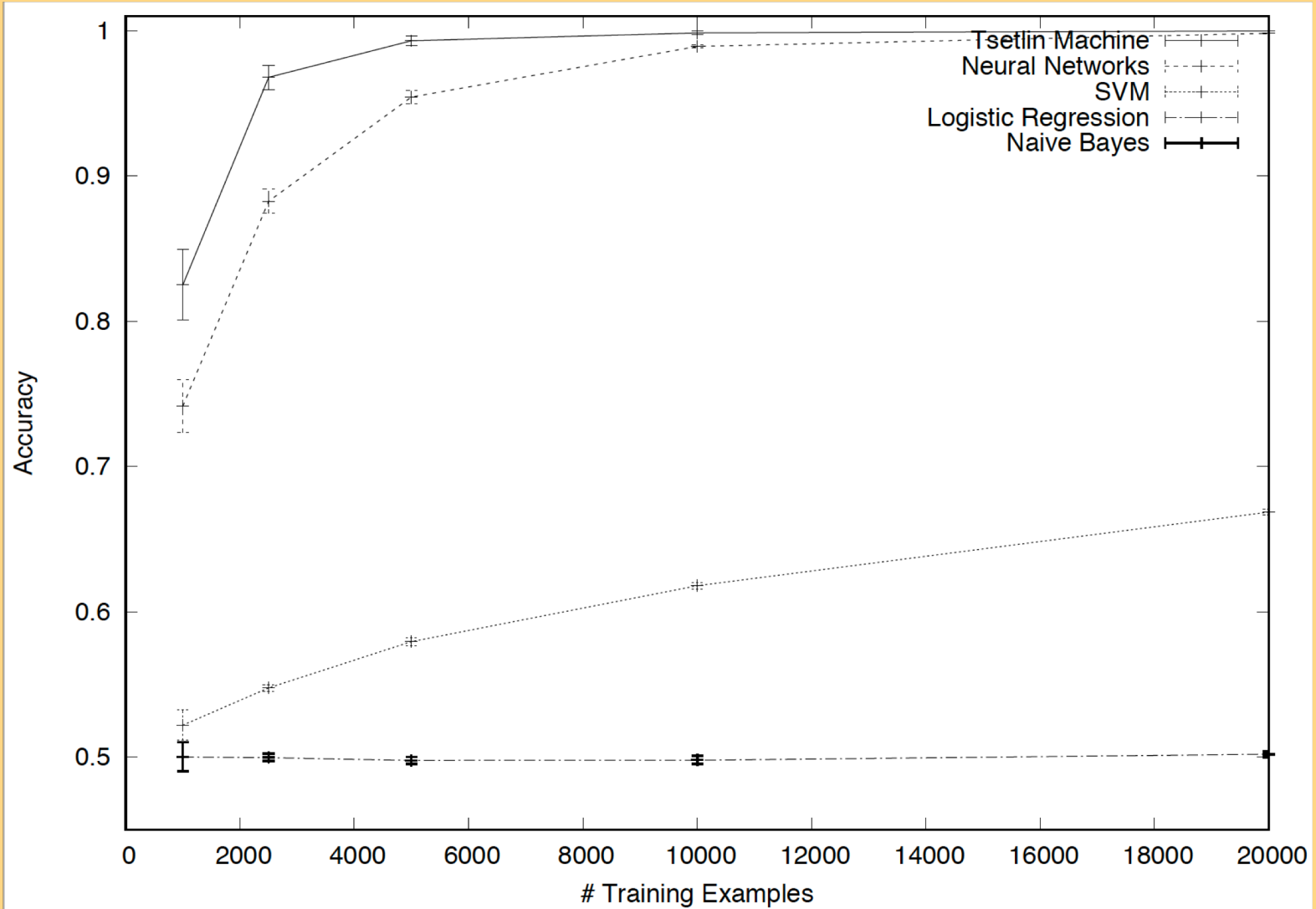


Input	Target
010110110110	1
111010110011	0
001101111010	0
101010111011	0
111011101100	1
10000010110	1
111011100010	0
101010111011	1
000011011100	0
100010110010	1

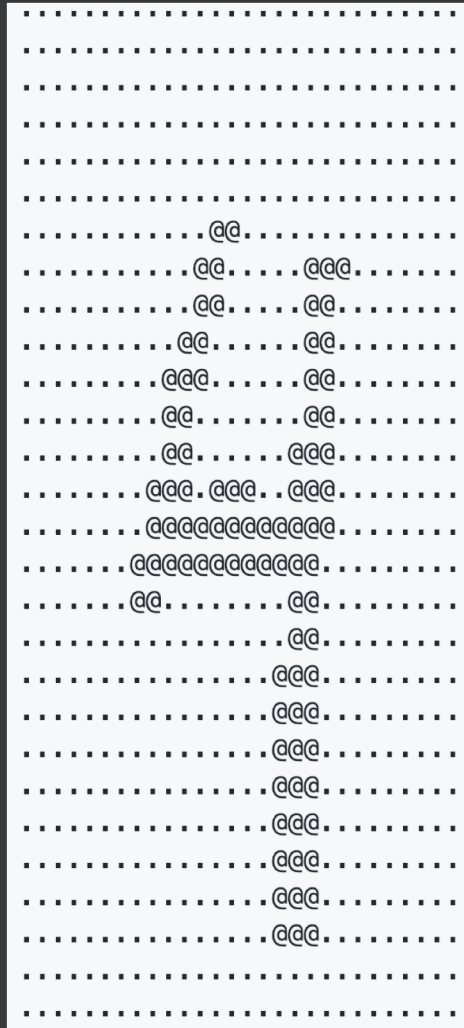
Noisy XOR dataset

Input	Target
010110110110	1
111010110011	0
001101111010	0
1010101111011	0
1110111101100	1
100000010110	1
111011100010	0
1010101111011	1
000011011100	0
100010110010	1

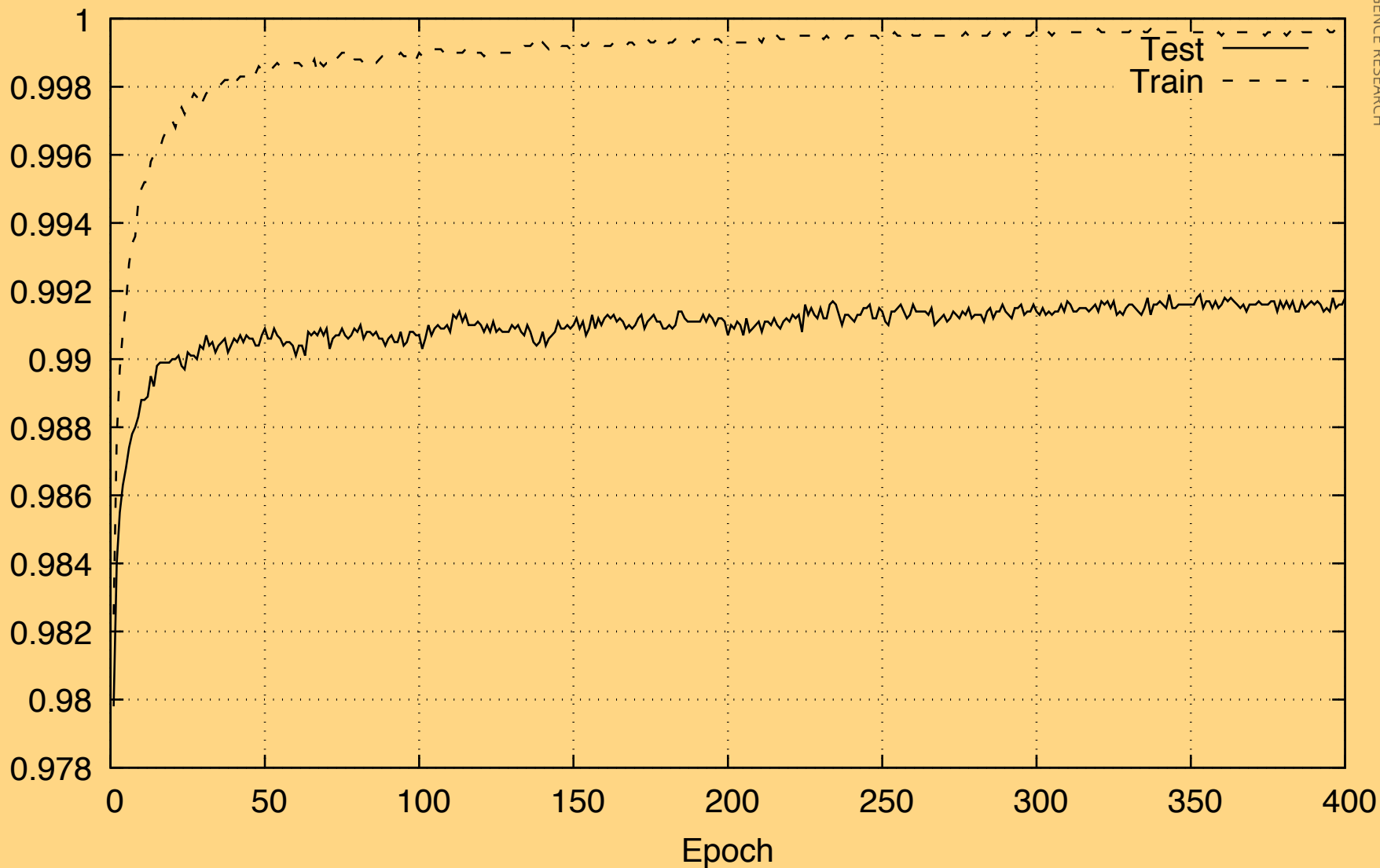
Noisy XOR dataset



Using the Tsetlin Machine to classify handwritten digits



Learning behaviour



Results on raw, unenhanced, and unextended MNIST data

Technique	Accuracy (%)
Convolutional Tsetlin Machine	99.2 ± 0.0
<i>2-layer NN, 800 HU, Cross-Entropy Loss</i>	98.6
Tsetlin Machine	98.2 ± 0.0
<i>K-nearest-neighbors, L3</i>	97.2
<i>3-layer NN, 500+150 hidden units</i>	97.1
<i>40 PCA + quadratic classifier</i>	96.7
<i>1000 RBF + linear classifier</i>	96.4
Logistic regression	91.5
<i>Linear classifier (1-layer NN)</i>	88.0
Decision tree	87.8
Multinomial Naive Bayes	83.2

Tsetlin Machine based text classification

Documents

1. He is allergic to Penicillin..
2. She reacts to Penicillin..



Terms	Document 1	Document 2
He	1	0
is	1	0
allergic	1	0
to	1	1
Penicillin	1	1
She	0	1
Reacts	0	1
..



Bit vectors

Document 1: 1111100..

Document 2: 0001111..

If not “don’t” and “react” and “Voltaren” then Allergy

Text understanding with human interpretable rules

Method	Precision	Recall	F-measure
Multinomial Naïve Bayes	85.9±0.0	86.1±0.0	86.0±0.0
Logistic regression	86.5±0.0	87.6±0.0	87.1±0.0
Decision tree	71.1±0.0	68.4±0.0	69.7±0.0
Random forest	78.9±0.1	78.1±0.1	78.5±0.1
kNN	58.4±0.0	63.5±0.0	60.8±0.0
Linear SVM	88.0±0.0	89.1±0.0	88.5±0.0
MLP	82.6±0.1	82.6±0.1	82.6±0.1
LSTM	87.2±0.7	84.3±0.9	85.6±0.6
LSTM CNN	89.5±0.2	86.8±0.4	88.1±0.1
Bi-LSTM	87.6±0.8	83.9±1.1	85.5±0.6
Bi-LSTM CNN	88.3±0.2	87.5±0.5	87.9±0.2
Tsetlin Machine	89.7±0.0	89.7±0.0	89.7±0.0

if “rash” and “reaction” and “penicillin” then Allergy

Tsetlin Machine – current activities

CAIR



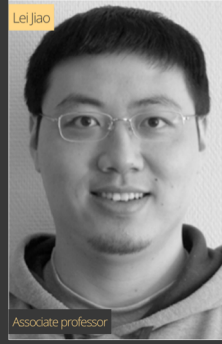
Recurrent Tsetlin Machine



Convolutional Tsetlin Machine



Hydropower optimization



Theoretical analysis



Natural language understanding



EKG analysis



Medical applications



Cause and effect

House of CAIR



Adaptive and scalable hardware, Newcastle University



Reinforcement learning, University of Groningen



Hardware, Temporal Computing, UK